

Unitarity cutting rules for hard processes on nuclear targets

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Outline

Overview: nonlinear k_{\perp} -factorization

Nuclear collective glue and its unitarity cut interpretation

Standard Abramovskii-Gribov-Kancheli (AGK) vs. QCD

Summary

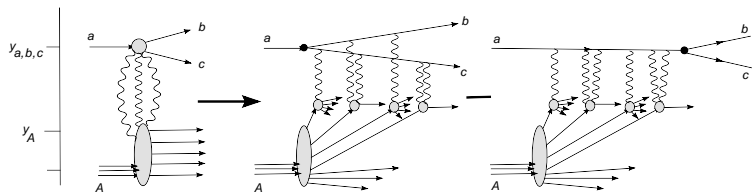


N.N. Nikolaev & W.S.

Unitarity cutting rules and topological cross sections in hard production off nuclei from nonlinear k_{\perp} -factorization.

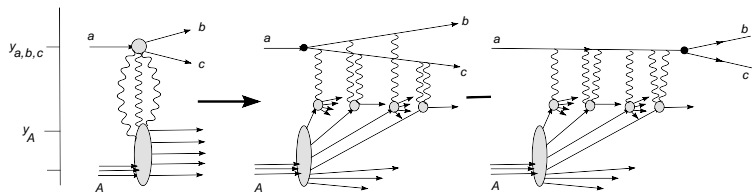
Phys. Rev. D74, 074021 (2006).

Production as excitation of beam partons $a \rightarrow bc$



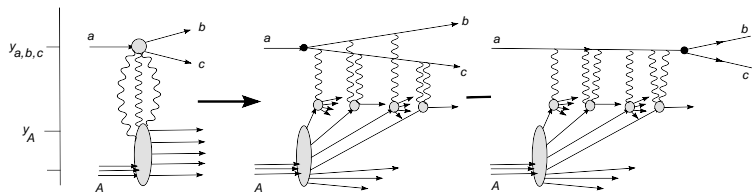
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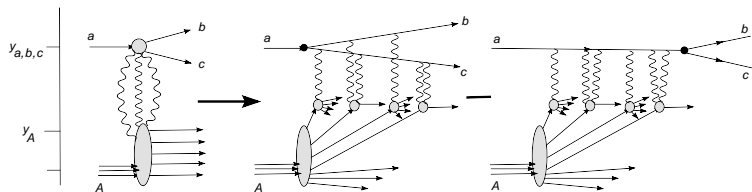
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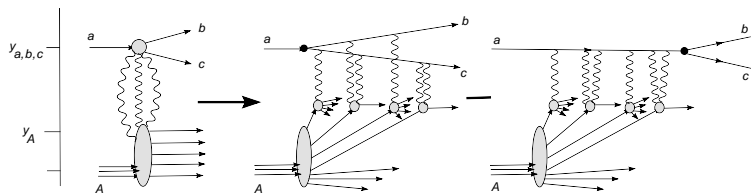
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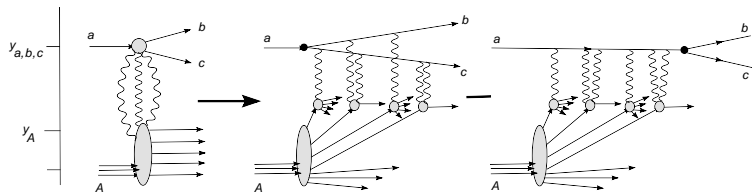
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- Nuclear target as a testing ground for unitarity/rescattering effects in hadronic hard interactions.

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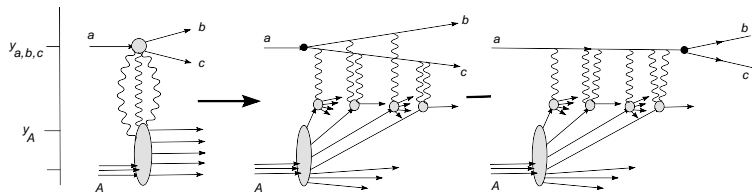
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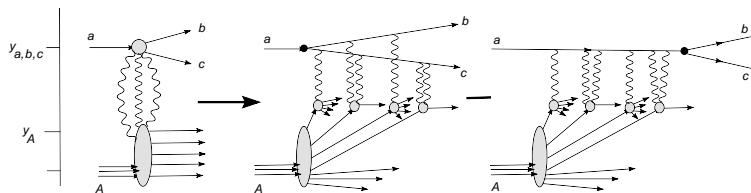
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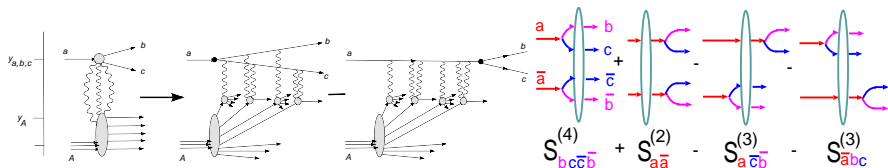
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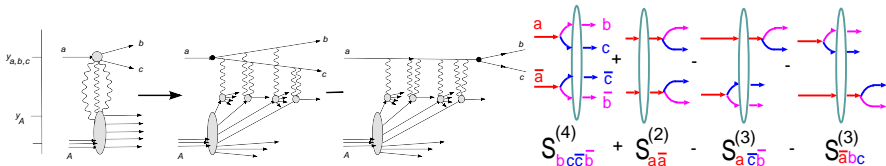
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- predictions for: cut pomeron/topological cross sections; forward-backward correlations; centrality/multiplicity dependence of hard interactions.

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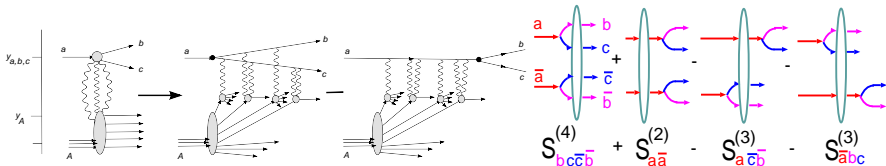
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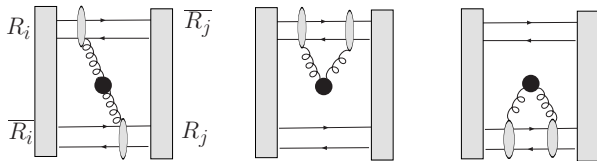
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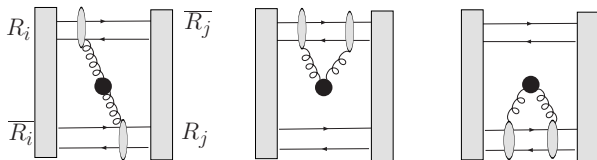
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- **first** square, average over target states, and apply closure in summing over the nucleon and nucleus excitation.
- **then** the problem reduces to the calculation of few-particle S -matrices in a color-coupled channel Glauber-Gribov multiple scattering theory.

Four parton dipole cross section operator:



- A matrix in the space of possible $SU(N)$ -color singlets.

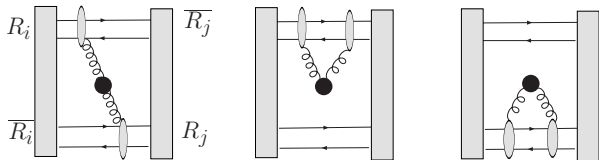
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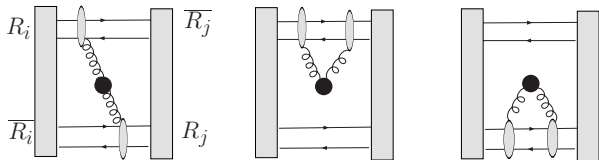
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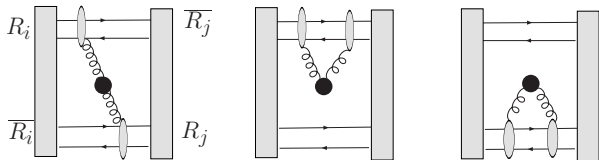


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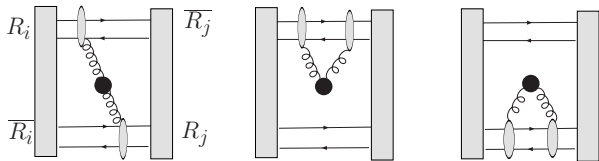


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- Only the sum will be infrared safe, separation into color excitations and elastic rescatterings is infrared sensitive.

Master formula for dijets

$$\frac{d\sigma(a^* \rightarrow bc)}{dz_b d^2\mathbf{p}_b d^2\mathbf{p}_c} = \int \frac{d^2\mathbf{b}_b d^2\mathbf{b}_c d^2\mathbf{b}'_b d^2\mathbf{b}'_c}{(2\pi)^4} e^{-i\mathbf{p}_b(\mathbf{b}_b - \mathbf{b}'_b) - i\mathbf{p}_c(\mathbf{b}_c - \mathbf{b}'_c)}$$
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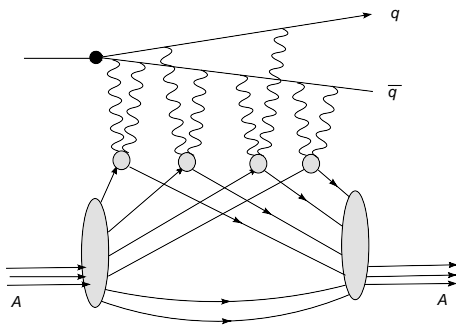
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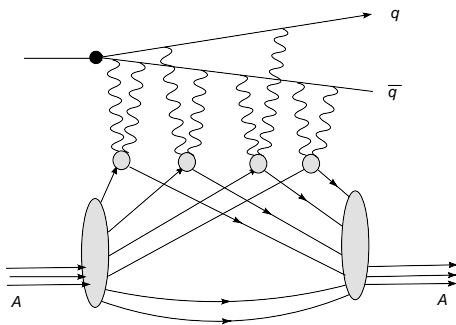
- Central dijets $g \rightarrow gg \implies \underbrace{1}_{1(N_c\text{-suppressed})} + \underbrace{8_A + 8_S}_{N_c^2} + \underbrace{10 + \bar{10} + 27 + R_7}_{N_c^2 \times N_c^2}$

Diffractive dijets define nuclear unintegrated gluon



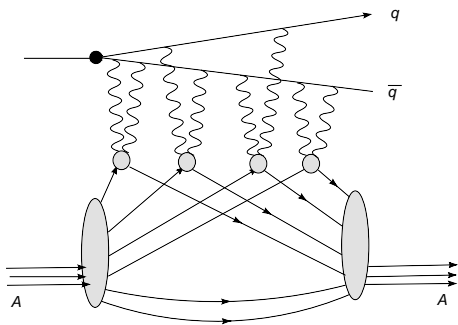
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- Diffractive hard dijets from pions:
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- Hard jets acquire \mathbf{p}_\perp from gluons
- Collective glue is a physical observable: $M_A(\mathbf{p}) \propto \phi(\mathbf{b}, \mathbf{p})$.

Nuclear unintegrated glue

- nuclear coherent glue per unit area in impact parameter space:

$$\phi(\mathbf{b}, \boldsymbol{\kappa}) = \sum w_j(\mathbf{b}) f^{(j)}(\boldsymbol{\kappa})$$

- collective glue of j overlapping nucleons :

$$f^{(j)}(\boldsymbol{\kappa}) = \int \left[\prod_{i=1}^j d^2 \boldsymbol{\kappa}_i f(\boldsymbol{\kappa}_i) \right] \delta(\boldsymbol{\kappa} - \sum \boldsymbol{\kappa}_i)$$

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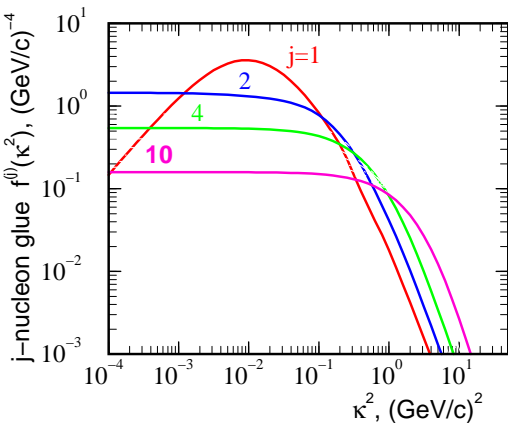
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Nuclear unintegrated glue: salient features

collective glue $f^{(j)}(\kappa)$

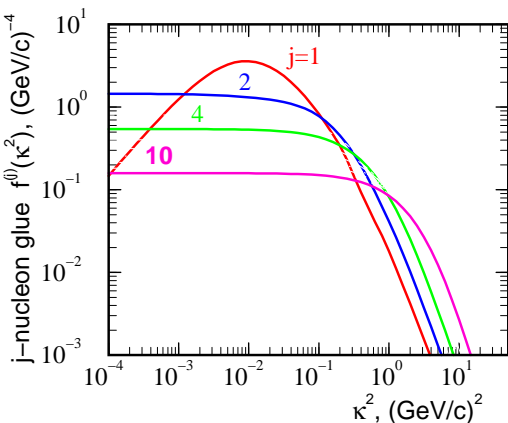


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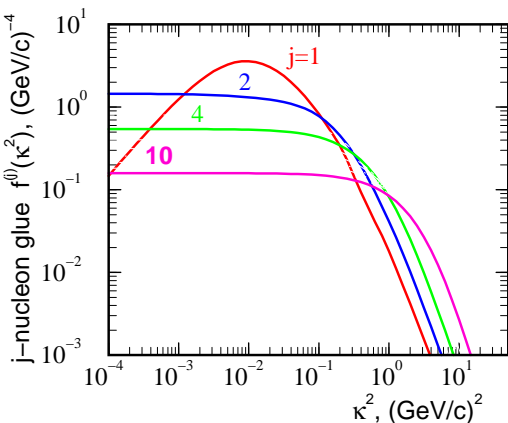
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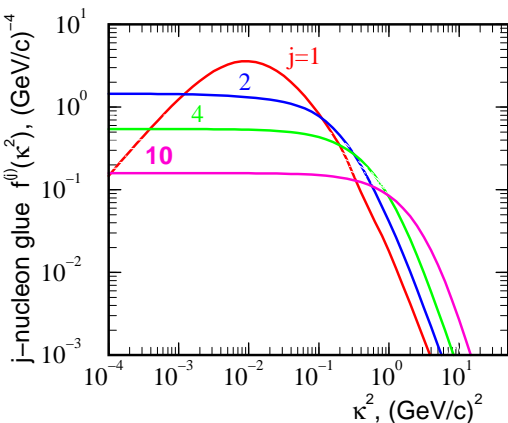
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- typical scale: the saturation scale $Q_A^2 \sim 0.8 \div 1 \text{ GeV}^2$ for realistic glue and heavy nuclei.
- large- κ^2 Cronin-type antishadowing enhancement
- furnishes linear k_{\perp} -factorization of inclusive deep inelastic, forward jets in DIS, and diffractive dijets.

Nuclear unintegrated glue: small- x evolution

- unintegrated glue:

$$\Phi(\mathbf{b}, x, \mathbf{p}) \equiv \int \frac{d^2\mathbf{r}}{(2\pi)^2} \exp[-i\mathbf{p}\mathbf{r}] S_{q\bar{q}}(\mathbf{b}, x, \mathbf{r}) = w_0 \delta^{(2)}(\mathbf{p}) + \phi(\mathbf{b}, x, \mathbf{p})$$

- small- x evolution *Nikolaev, Zakharov, Zoller / Mueller'94:*

$$S_{q\bar{q}}(\mathbf{b}, x_0, \mathbf{r}) \rightarrow S_{q\bar{q}}(\mathbf{b}, x_0, \mathbf{r}) + \log(x_0/x) \delta S_{q\bar{q}}(\mathbf{b}, x, \mathbf{r})$$
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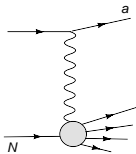
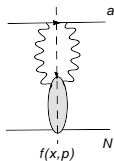
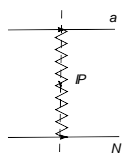
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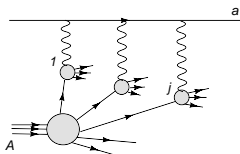
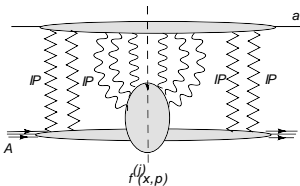
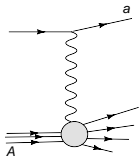
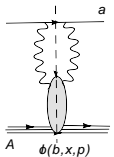
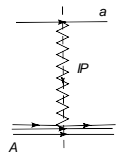
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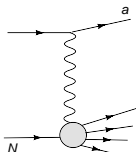
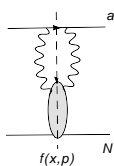
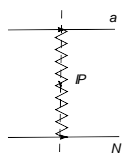
Unitarity cut interpretation of the nuclear glue



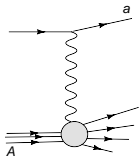
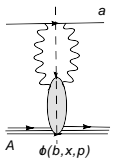
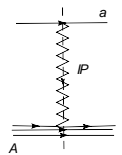
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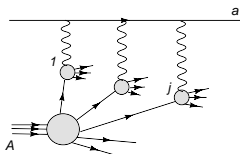
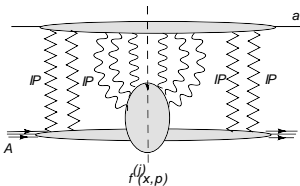
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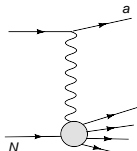
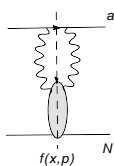
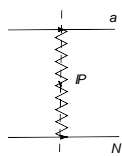
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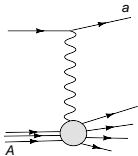
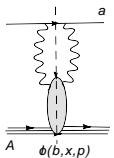
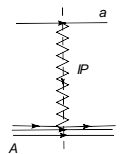
- Expansion of the cut nuclear pomeron in the cut free-nucleon pomerons



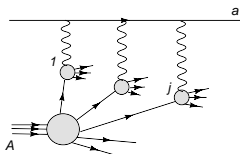
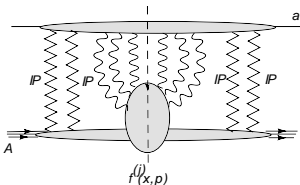
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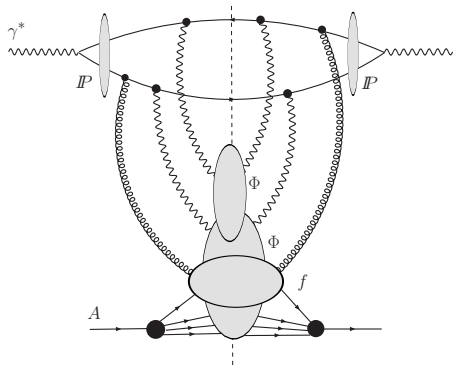
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- Expansion of the cut nuclear pomeron in the cut free-nucleon pomerons
- Screening by uncut pomerons in the expansion coefficients

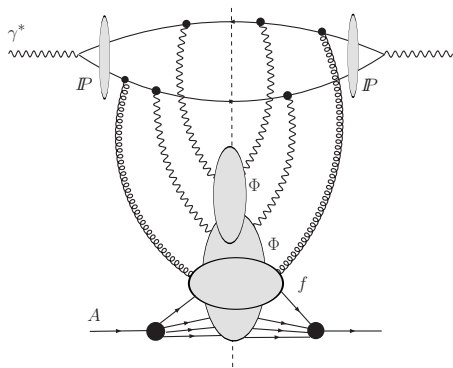


Uncut, and two types of cut Pomeron



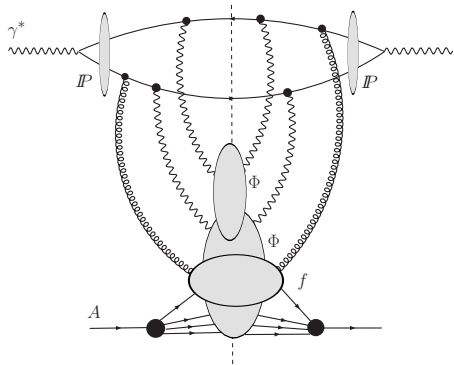
- coherent distortion of lightcone WF \rightarrow uncut Pomeron exchanges.

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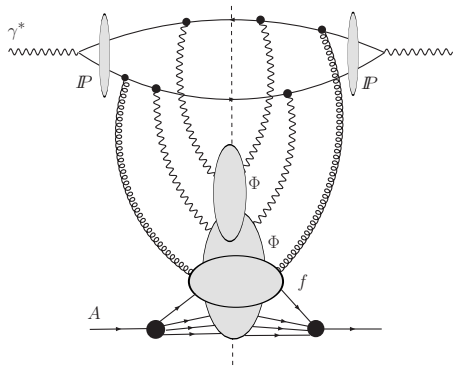
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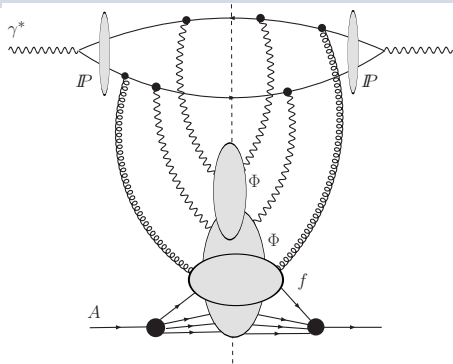
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 - transitions between two multiplets of different dimensionality (here $1 \rightarrow 8$): necessarily leaves a color excited nucleon, coupling $\propto T_A(\mathbf{b})f(x, \kappa)$, couples to both constituents.

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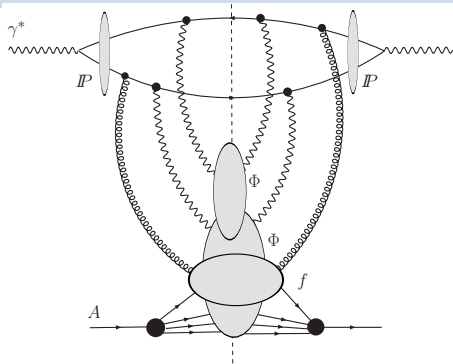
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 - rotations within the same color multiplet: summed up in the nuclear Reggeons. Coupling $\propto \Phi(\mathbf{b}, x, \kappa_i)$.

Uncut, and two types of cut Pomeron



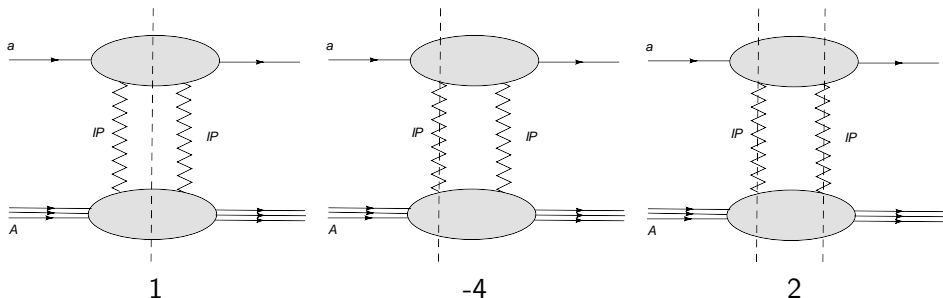
- A color rotation Pomeron contributes j color excited nucleons with a weight $\propto w_j(\mathbf{b}) f^{(j)}(x, \kappa_i)$.

Uncut, and two types of cut Pomeron



- A color rotation Pomeron contributes j color excited nucleons with a weight $\propto w_j(\mathbf{b}) f^{(j)}(x, \kappa_i)$.
- Even for single-particle spectra, in topological cross sections, *spectator interactions leave a trace*

QCD vs. standard AGK: two-Pomeron cuts

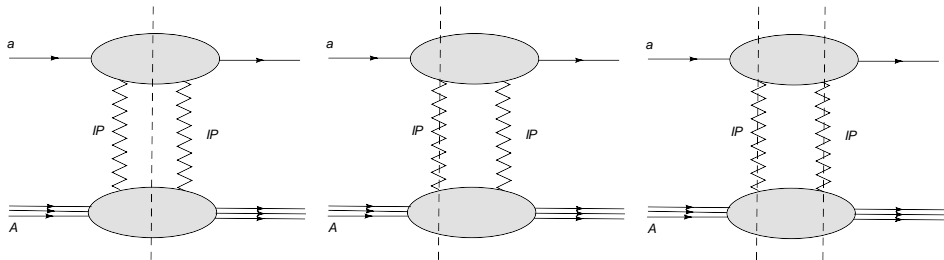


- AGK for DIS off a nucleus:

$$\Delta_2 \Gamma_2^{in}(\cancel{\mathbf{P}\mathbf{P}}; \mathbf{b}, \mathbf{r}) = -[\sigma(x, \mathbf{r}) T(\mathbf{b})]^2$$

$$\Delta_2 \Gamma_D(\mathbf{P}\mathbf{P}; \mathbf{b}, \mathbf{r}) : \Delta_2 \Gamma_1^{in}(\cancel{\mathbf{P}\mathbf{P}}; \mathbf{b}, \mathbf{r}) : \Delta_2 \Gamma_2^{in}(\cancel{\mathbf{P}\mathbf{P}}; \mathbf{b}, \mathbf{r}) = 1 : -4 : 2$$

QCD vs. standard AGK: two-Pomeron cuts



- QCD: the cut pomerons couple differently to **singlet-to-octet excitation** and **octet-to-octet rotation**:

$$\Delta_2 \Gamma_1^{in} \left(\begin{array}{c} \text{IP} \\ \text{IP} \\ \text{e} \end{array} ; \mathbf{b}, \mathbf{r} \right) = -\frac{1}{2} \cdot [\sigma_0(x) T(\mathbf{b})] \cdot [\sigma(x, \mathbf{r}) T(\mathbf{b})] - \frac{1}{2} [\sigma(x, \mathbf{r}) T(\mathbf{b})]^2$$

$$\Delta_2 \Gamma_2^{in} \left(\begin{array}{c} \text{IP} \\ \text{IP} \\ \text{r} \\ \text{e} \end{array} ; \mathbf{b}, \mathbf{r} \right) = \frac{1}{2} \cdot [\sigma_0(x) T(\mathbf{b})] [\sigma(x, \mathbf{r}) T(\mathbf{b})]$$

QCD vs. standard AGK: topological cross sections

Inelastic cross section of the $q\bar{q}$ -dipole-Nucleus interaction:

$$\begin{aligned}\Gamma^{inel}(\mathbf{r}, \mathbf{b}) &= 1 - \exp[-\sigma(\mathbf{r})T(\mathbf{b})] \\ &= \exp[-\sigma(\mathbf{r})T(\mathbf{b})] \sum_{\nu} \frac{1}{\nu!} [\sigma(\mathbf{r})T(\mathbf{b})]^{\nu}\end{aligned}$$

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- Following Capella-Kaidalov-Bertocchi-Treleani:

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- Invalid in QCD. Ignores the role of spectator interactions and the two types of cut Pomerons.
- Spectrum of forward quarks in DIS. ν cut Pomerons affect x_F distribution:

$$\frac{d\sigma_{\nu}}{d^2\mathbf{b}dx_F} = \int d^2\mathbf{r} \left| \psi(x_F, \mathbf{r}) \right|^2 \Gamma^{(\nu)inel}(\mathbf{r}, \mathbf{b})$$

Summary

- Topological cross sections follow directly from nonlinear- k_{\perp} factorization for inclusive cross sections
- Novel property of QCD unitarity cutting rules: two kinds of cut pomerons
- Comover/spectator interactions contribute to topological cross sections